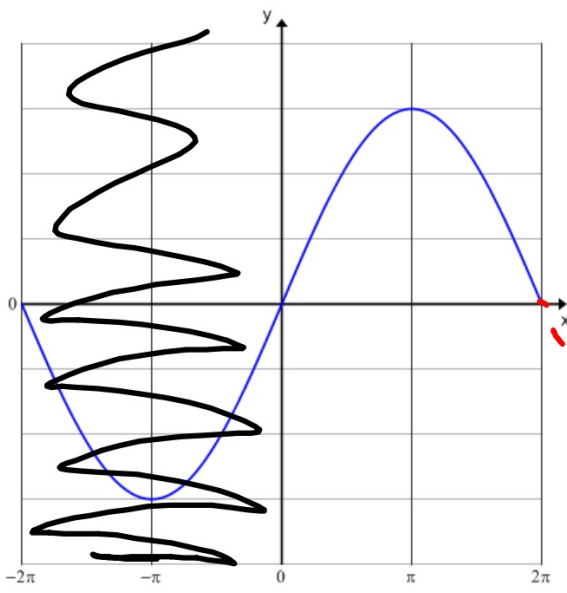
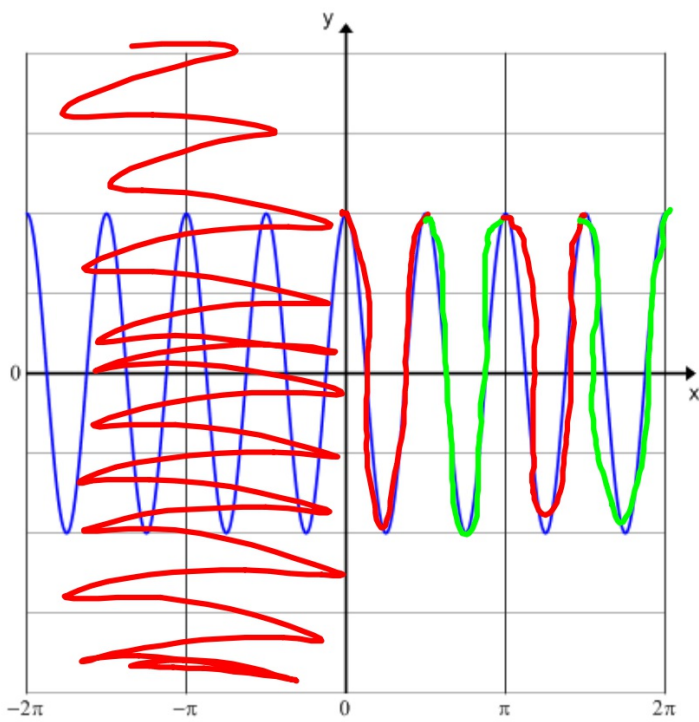


$$y = \frac{1}{2} \sin(2\theta)$$



$$y = 3 \sin\left(\frac{1}{2}x\right)$$



$$y = 2\cos(4x)$$

$$\textcircled{1} \quad y = 3 \sin(2\theta - 12^\circ)$$

$$\text{Amplitude} = 3$$

$$\text{Period} = \frac{360}{2} = 180^\circ$$

$$\text{Phase shift} = \frac{-c}{b} = \frac{-(-12)}{2} = 6^\circ$$

$$\textcircled{2} \quad y = 5 \cos\left(\frac{1}{4}\theta + 8^\circ\right)$$

$$\text{Amplitude} = 5$$

$$\text{Period} = \frac{360}{\frac{1}{4}} = 1440^\circ$$

$$\text{Phase shift} = \frac{-c}{b} = \frac{-8}{\frac{1}{4}} = -32^\circ$$

- $\textcircled{3}$ Give sine graph that has amplitude of 4, period of 90, and phase shift of 4° .

$$y = 4 \sin\left(\frac{4}{1}\theta - 16\right)$$

$$\text{period} = \frac{360}{b}$$

$$\frac{90}{1} = \frac{360}{b}$$

$$\frac{90b}{90} = \frac{360}{90}$$

$$b = 4$$

$$\text{p.s.} = \frac{-c}{b}$$

$$\frac{4}{1} = \frac{-c}{4}$$

$$-c = 16$$

$$c = -16$$

④ Sine equation with

$$A = 2 \quad \text{Period} = 720 \quad \text{P.S.} = 8^\circ$$

$$y = 2 \sin\left(\frac{1}{b}\theta - \frac{c}{c}\right)$$

$$P = \frac{360}{b}$$

$$\frac{720}{1} = \frac{360}{b}$$

$$\frac{720b}{720} = \frac{360}{720}$$

$$b = \frac{1}{2}$$

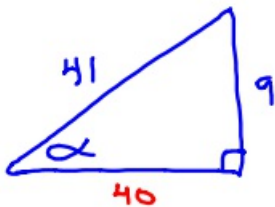
$$\text{p.s.} = \frac{-c}{b}$$

$$\frac{8}{1} = \frac{-c}{\frac{1}{2}}$$

$$-c = 4$$

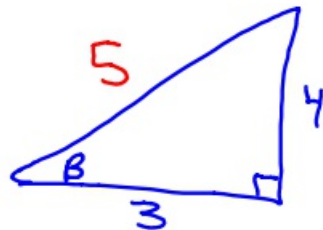
$$c = -4$$

⑤ If $\sin \alpha = \frac{9}{41}$ and $\tan \beta = \frac{4}{3}$,
find $\cos(\alpha - \beta)$.



$$a^2 + 9^2 = 41^2$$

$$a = 40$$



$$3^2 + 4^2 = c^2$$

$$25 = c^2$$

$$5 = c$$

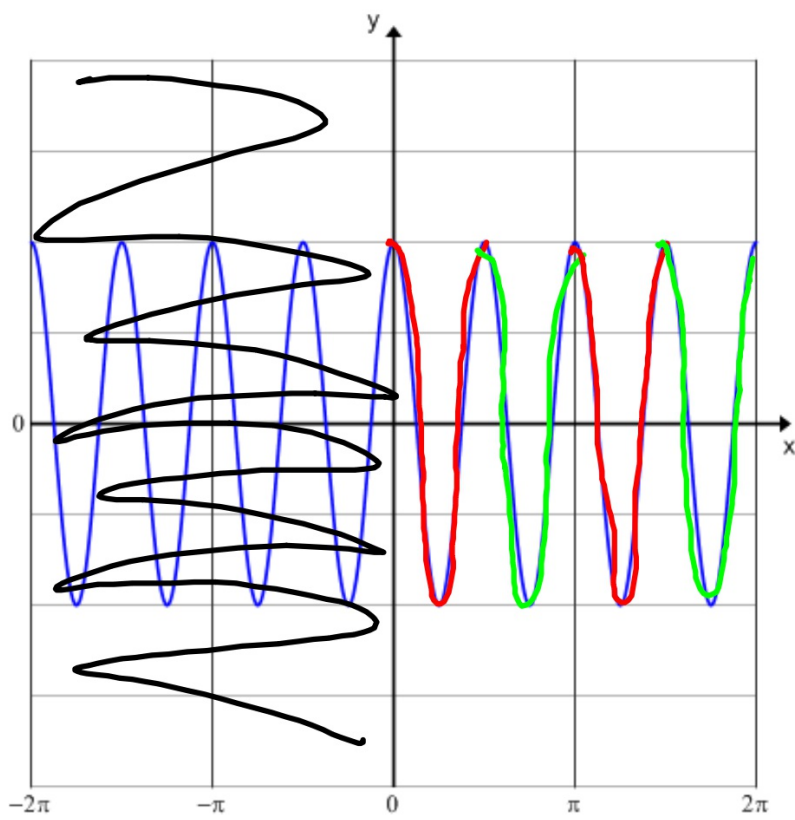
$$\cos(\alpha - \beta) = \cos \alpha \cdot \cos \beta + \sin \alpha \cdot \sin \beta$$

$$\frac{40}{41} \cdot \frac{3}{5} + \frac{9}{41} \cdot \frac{4}{5}$$

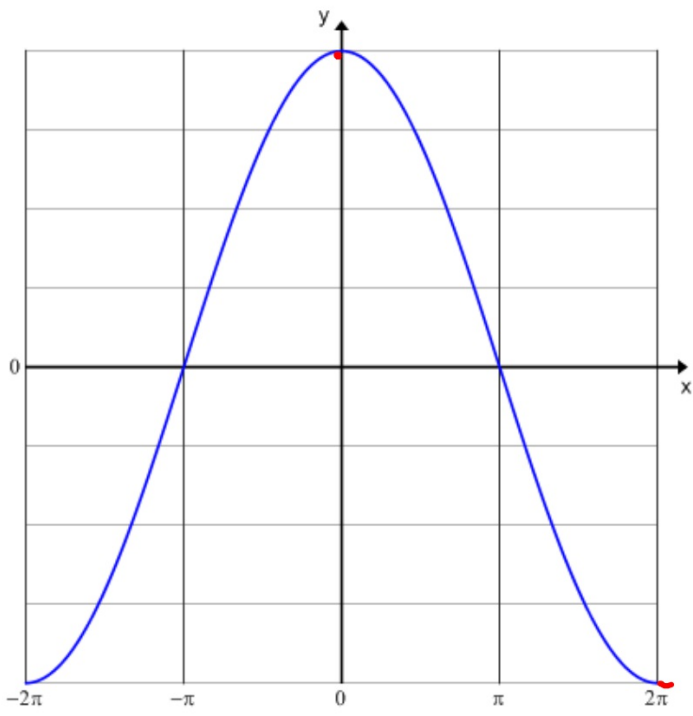
$$\frac{120}{205} + \frac{36}{205}$$

$$\frac{156}{205}$$

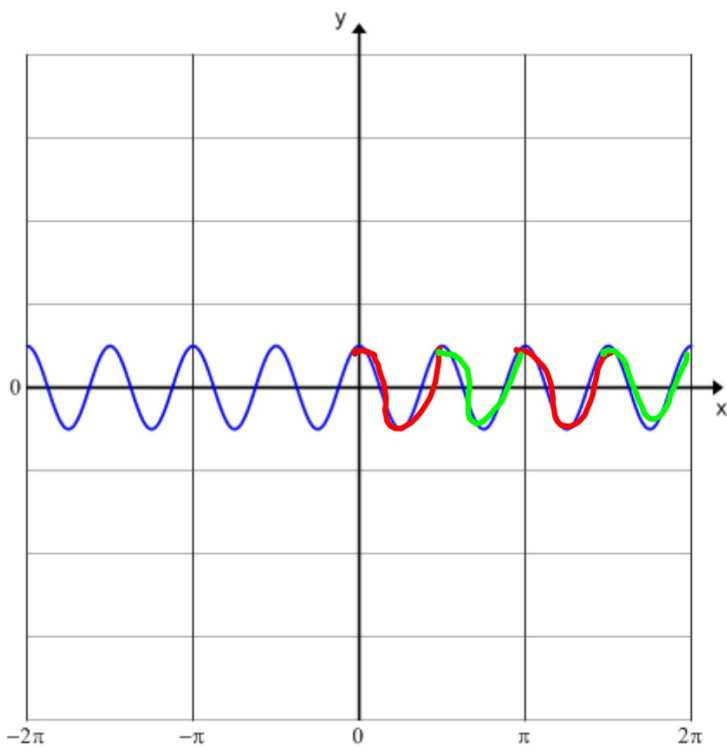
4-5-18 3rd Trig



$$y = 2 \cos(4\theta)$$



$$y = 4 \cos\left(\frac{1}{2}\theta\right)$$



$$y = \frac{1}{2} \cos(4\theta)$$

$$\textcircled{1} \quad y = 4 \cos\left(\frac{2}{b}\theta + \frac{8}{c}\right)$$

$$\text{Amplitude} = 4$$

$$\text{Period} = \frac{360}{2} = 180^\circ$$

$$\text{Phase shift} = \frac{-c}{b} = \frac{-8}{2} = -4$$

$$\textcircled{2} \quad y = \sin\left(\frac{1}{2}\theta + 4\right)$$

$$\text{Amplitude} = 1$$

$$\text{Period} = \frac{360}{\frac{1}{2}} = 720^\circ$$

$$\text{Phase shift} = \frac{-c}{b} = \frac{-4}{\frac{1}{2}} = -8$$

$\textcircled{3}$ Give me the Sine equation that has

$$\text{Amplitude} = 2 \quad \text{Period} = 90^\circ \quad \text{Phase shift} = 12^\circ$$

$$y = 2 \sin(4\theta - 48)$$

$$\text{period} = \frac{360}{b}$$

$$\frac{90}{1} = \frac{360}{b}$$

$$90b = 360$$

$$b = 4$$

$$\text{P.S.} = \frac{-c}{b}$$

$$\frac{12}{1} = \frac{-c}{4}$$

$$-c = 48$$

$$c = -48$$

④ Sine eq w/ Period = 720° P.S. = -4

$$y = \sin\left(\frac{1}{b}\theta + \frac{c}{b}\right)$$

$$\text{Period} = \frac{360}{b}$$

$$\text{P.S.} = \frac{-c}{b}$$

$$\frac{720}{1} = \frac{360}{b}$$

$$\frac{-4}{1} = \frac{-c}{\frac{1}{2}}$$

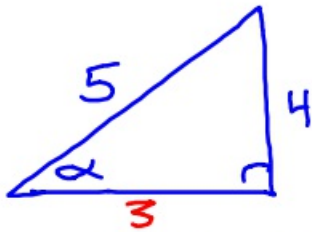
$$\frac{720b}{720} = \frac{360}{720}$$

$$-c = -2$$

$$b = \frac{1}{2}$$

$$c = 2$$

⑤ If $\sin \alpha = \frac{4}{5}$ and $\tan \beta = \frac{5}{12}$,
find $\cos(\alpha - \beta)$.

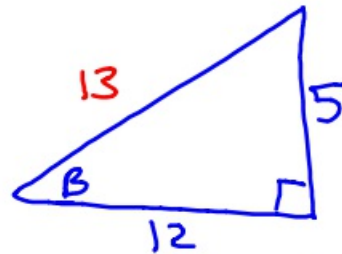


$$a^2 + 4^2 = 5^2$$

$$a^2 + 16 = 25$$

$$a^2 = 9$$

$$a = 3$$



$$12^2 + 5^2 = c^2$$

$$169 = c^2$$

$$c = 13$$

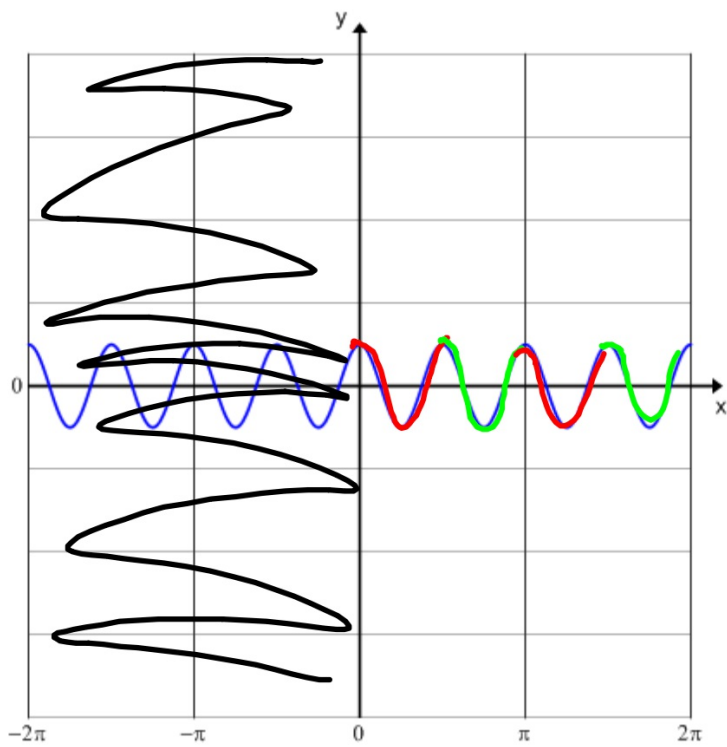
$$\cos(\alpha - \beta) = \cos \alpha \cdot \cos \beta + \sin \alpha \cdot \sin \beta$$

$$\frac{3}{5} \cdot \frac{12}{13} + \frac{4}{5} \cdot \frac{5}{13}$$

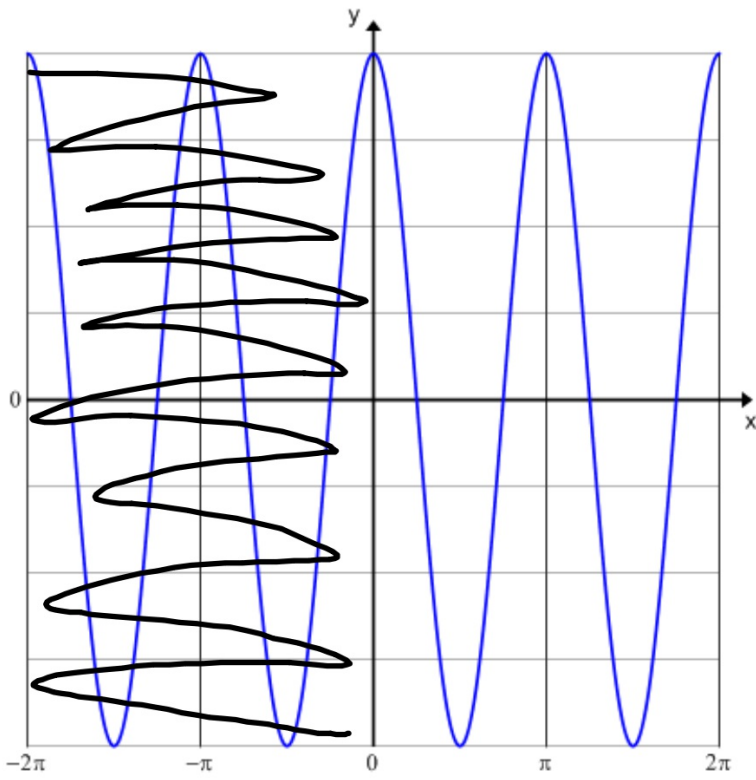
$$\frac{36}{65} + \frac{20}{65}$$

$$\frac{56}{65}$$

4-5-18 4^{ta} Trig



$$y = \frac{1}{2} \cos\left(\frac{4}{b} \theta\right)$$



$$y = 4 \cos(2\theta)$$

$$\textcircled{1} \quad y = 8 \sin\left(\frac{4}{b}\theta + 12\right)$$

$$\text{amplitude} = 8$$

$$\text{period} = \frac{360}{b} = \frac{360}{4} = 90^\circ$$

$$\text{phase shift} = -\frac{c}{b} = -\frac{12}{4} = -3$$

$$\textcircled{2} \quad y = \cos\left(\frac{1}{2}\theta + 4\right)$$

$$\text{Amplitude} = 1$$

$$\text{Period} = \frac{360}{\frac{1}{2}} = 720^\circ$$

$$\text{Phase Shift} = -\frac{c}{b} = -\frac{4}{\frac{1}{2}} = -8$$

$\textcircled{3}$ Give the sine equation that has amplitude = 4, period = 180° , and phase shift = 16.

$$y = 4 \sin\left(\frac{2}{b}\theta - \frac{32}{c}\right)$$

$$\text{period} = \frac{360}{b}$$

$$\frac{180^\circ}{1} = \frac{360}{b}$$

$$180b = 360$$

$$b = 2$$

$$\text{p.s.} = -\frac{c}{b}$$

$$\frac{16}{1} = -\frac{c}{2}$$

$$-c = 32$$

$$c = -32$$

- ④ Give sine equation with
period = 720° + phase shift = 6.

$$y = \sin\left(\frac{1}{b}\theta - \frac{c}{c}\right)$$

$$p = \frac{360}{b}$$

$$\frac{720}{1} = \frac{360}{b}$$

$$720b = 360$$

$$b = \frac{1}{2}$$

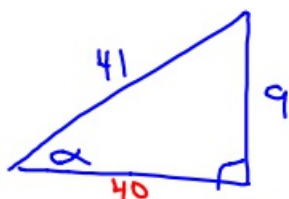
$$p.s. = \frac{-c}{b}$$

$$\frac{6}{1} = \frac{-c}{\frac{1}{2}}$$

$$-c = 3$$

$$c = -3$$

- ④ If $\sin \alpha = \frac{9}{41}$ and $\cos B = \frac{5}{13}$,
find $\cos(\alpha - B)$.

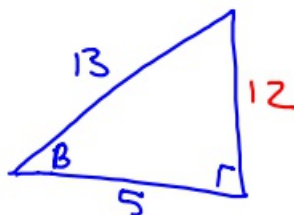


$$a^2 + 9^2 = 41^2$$

$$a^2 + 81 = 1681$$

$$a^2 = 1600$$

$$a = 40$$



$$5^2 + b^2 = 13^2$$

$$25 + b^2 = 169$$

$$b^2 = 144$$

$$b = 12$$

$$\cos(\alpha - B) = \cos \alpha \cdot \cos B + \sin \alpha \cdot \sin B$$

$$\frac{40}{41} \cdot \frac{5}{13} + \frac{9}{41} \cdot \frac{12}{13}$$

$$\frac{200}{533} + \frac{108}{533}$$

$$\frac{308}{533}$$