

# 7-4 Intercepts and Discriminants

Name: \_\_\_\_\_

Time Start: \_\_\_\_\_ Finish: \_\_\_\_\_ Total Time = \_\_\_\_\_

In 1-5, find the x-intercepts and the y-intercepts of the given equations.

1.  $f(x) = x^2 + 8x - 9$       x-intercept = \_\_\_\_\_      y-intercept = \_\_\_\_\_

2.  $f(x) = 3x - 9$       x-intercept = \_\_\_\_\_      y-intercept = \_\_\_\_\_

3.  $f(x) = x^2 + 6x + 5$       x-intercept = \_\_\_\_\_      y-intercept = \_\_\_\_\_

4.  $f(x) = 4x^2 - 7x - 2$       x-intercept = \_\_\_\_\_      y-intercept = \_\_\_\_\_

5.  $f(x) = x^3 + 2x^2 - x - 2$       x-intercept = \_\_\_\_\_      y-intercept = \_\_\_\_\_

## Discriminants Section

Use the discriminant of each equation to determine how many solutions exist.

1.  $3x^2 - x - 8 = 0$   
Number of solutions = \_\_\_\_\_

2.  $2x^2 - 4x + 2 = 0$   
Number of solutions = \_\_\_\_\_

3.  $x^2 - 3x - 10 = 0$   
Number of solutions = \_\_\_\_\_

4.  $4x^2 + x + 10 = 0$   
Number of solutions = \_\_\_\_\_

5. Consider the equation  $x^2 - 6x + 13 = 0$ . No real number solutions exist.  
Thus, the equation  $f(x) = x^2 - 6x + 13$  does not cross the x-axis – important concept.  
Determine the y-intercept and then calculate the derivative to find the vertex of the parabola.  
Now determine a third point on the parabola without plugging values into the equation.

y-intercept = \_\_\_\_\_      vertex = \_\_\_\_\_      3<sup>rd</sup> point = \_\_\_\_\_

6. Consider the equation  $x^2 + 2x + 2 = 0$ . No real number solutions exist.  
Thus, the equation  $f(x) = x^2 + 2x + 2$  does not cross the x-axis – important concept.  
Determine the y-intercept and then calculate the derivative to find the vertex of the parabola.  
Now determine a third point on the parabola without plugging values into the equation.

y-intercept = \_\_\_\_\_      vertex = \_\_\_\_\_      3<sup>rd</sup> point = \_\_\_\_\_

## SAT Questions

\_\_\_\_\_ 7. If  $\frac{x}{2} = y$  and  $2y = y$ , what is the value of  $x$ ?

\_\_\_\_\_ 8. The average (arithmetic mean) of  $x$  and  $y$  is  $m$ , where  $m \neq 0$ .  
What is the average (arithmetic mean) of  $x$ ,  $y$ , and  $2m$ ?

- A.  $m$       B.  $\frac{4}{3}m$       C.  $\frac{3}{2}m$       D.  $\frac{5}{3}m$       E.  $2m$

\_\_\_\_\_ 9. If  $5x^2 - 15x = 0$  and  $x \neq 0$ , find the value of  $x$ .

\_\_\_\_\_ 10. If  $n = 5^{2000} + 5^{2002}$ , then what are the prime factors of  $n$ ?

- A. 5 only  
B. 2 and 5 only  
C. 2, 5, and 10 only  
D. 2, 5, and 13 only  
E. 2, 5, 1000, and 1001 only